

## Phase 1: First Attempt

- Identify the problem
  - How many parameters are there?
  - What type of input values? What type of output values?
    - Numbers, characters, strings, sets, sequence, tuple, graph
  - Create a clear example of the inputs and outputs
    - Small example inputs
    - Boundary values (e.g., super large integers)
    - Uncommon values
      - Negative numbers, prime numbers
      - Whitespace characters, symbols and digits in strings
  - If it's strings
    - Am I allowed to treat strings as primitives, or will I have to consider string comparisons (which are linear time)
  - If it is a collection
    - Is it sorted/ordered?
    - Are duplicates allowed?
    - Is there a minimum size?
    - What is the element type?
  - Clearly restate the problem in my own words
  - Make a graphical representation of the problem
  - Is it a decision problem, search problem, or optimization problem?
    - Keep an eye out for the exact kind of output - often decision problems are easier than search problems.
- Define the context
  - What runtime are they expecting?
    - If it is constant time, I should think about:
      - Positional access of an array (all cases)
      - Accessing an element in a Hash Table (expected case)
      - Adding/Popping an element to a linked list
      - Check if an element is in a Hash Set
      - Checking the maximum/minimum of a heap
    - If it logarithmic time, maybe I need:
      - Self-balancing Binary Search Tree lookup/removal/addition
      - Removing/Adding an element to a Heap
      - Binary search of a linear data structure
      - Traversing to the bottom of a tree
    - If it is linear, I can probably use:
      - Linear data structures, like a list
      - Non-comparison based sorting algorithms
    - If it is linearithmic, I should think about:
      - Sorting the input
      - Constructing a balanced tree
    - If it is quadratic, I should think about:

- Crosswise comparison of two linear structures
  - What variables is the expected runtime expressed in?
    - Do I know the type of the variable?
      - Is it the size of a collection (n)?
      - Is it the number of bits in a number?
      - Is it the size of the number itself?
      - Is it the number of nodes in a tree?
    - Are there more than one variables?
    - Do any of the variables have any relationships?
  - Are they telling me anything about the best/expected/worst case?
    - If the worst case is different than the expected case, I should think about data structures with different behavior in those cases:
      - Amortized structures (e.g., vectors)
      - Hash maps
  - Do they demand a specific time complexity, or are they using Big Oh?
    - If it's a specific time complexity, then I have to use very precise methods and really keep an eye on my operations.
    - If it's Big Oh, then I should keep in mind that I can let bigger operations dominate
      - If I sort, then I can do any number of linear operations as long as there are not a linear number of them.
  - What about space complexity?
    - If it's constant space, probably have to do swaps and work with the data structures they already give me
    - If it's logarithmic space, then I can think about something like a callstack or a tree exploration that doesn't require much additional space
    - If it's linear space, I can have a linear data structure, but I can also fit them into a tree.
    - If it's quadratic, I think about tables
  - What other constraints does the problem impose?
    - Do they limit the number of comparisons I should do?
      - Start thinking about trees and tournaments
      - Use a Decision tree to enumerate the possible universes of input
    - Do they reference specific data structures I can key in on?
- Explore possible strategies
  - What is the dumbest possible brute-force solution that might work?
    - Could I generate every possible candidate solution and test if it works?
  - Is the data unsorted? What happens if I sort it?
    - Is the collection just integers? Can I use a non-comparison based sorting algorithm?
  - What happens if I put things into a Hash Map?
    - Can I have integer indices and use an array instead?
    - If I need to have multiple things tied to a key, should I use a set or a list?
  - What happens if I put things into a tree?

- I can often get a win if I have to end up traversing to the bottom of a tree instead of across all elements.
    - If I have to traverse, what order should I do it in?
  - Can I describe the problem with a graph?
    - What are the vertices and the edges?
    - Can I flip things around so that what I thought of as edges are now vertices?
  - Do I need to search a collection?
    - Is there any way I can build up the collection to have the value that I want, in a convenient location (e.g., the front or back).
    - What happens if I keep pointers between elements, can I short circuit having to do repeated traversals?
  - If I'm being restricted by time complexity, can I flatten operations to not happen inside of loops?
  - Can I swap out for a more/less restricted data structure?
    - E.g., can I replace a list with a Stack/Queue/Deque?
    - Does a Tree have to be self-balancing, or can I build it to be balanced as I go?
  - What if I reframe the problem recursively?
    - What are subproblems?
    - What is the base case?
    - How do I split up the problem?
    - How do I recombine the problem?
    - Where is the recursion?
- Act on the best solution
  - Let me try my solution on the example inputs I made before, carefully walking through and keeping mental track of the correctness and efficiency.
- Reflection
  - I found a solution, but was it fast enough?
  - Are any steps unnecessary?
  - Can I find a counterexample that proves my solution is wrong?

## Phase 2: Take a Break

- Ideally sleep for 8 hours

## Phase 3: Second Attempt

- Sit down and repeat Attempt 1 on all of this, limited to at least 30 minutes.
- Google the problem description that I have.
- Crack open the textbook and see if they have a relevant algorithm for this problem.

## Phase 4: Reflection

- Ask myself:
  - What worked well?
  - What failed?